DESIGN OF A SINGLE-PHASE RADIAL FLUX PERMANENT MAGNET GENERATOR WITH VARIATION OF THE STATOR DIAMETER

Hari Prasetijo*, Winasisa, Priswantoa, Dadan Hermawanb

aDepartment of Electrical Engineering, Faculty of Engineering, Jenderal Soedirman University, Purwokerto, Indonesia
bDepartment of Chemistry, Faculty of Sciences, Jenderal Soedirman University, Purwokerto, Indonesia

Article history
Received 13 June 2018
Received in revised form 11 April 2019
Accepted 16 April 2019
Published online 25 June 2019

*Corresponding author hari.prasetijo@unsoed.ac.id

Graphical abstract

Abstract

This study aims to observe the influence of the changing stator dimension on the air gap magnetic flux density ($B_g$) in the design of a single-phase radial flux permanent magnet generator (RFPMG). The changes in stator dimension were carried out by using three different wire diameters as stator wire, namely, AWG 14 ($d = 1.63$ mm), AWG 15 ($d = 1.45$ mm) and AWG 16 ($d = 1.29$ mm). The dimension of the width of the stator teeth ($W_{ts}$) was fixed such that a larger stator wire diameter will require a larger stator outside diameter ($D_{so}$). By fixing the dimensions of the rotor, permanent magnet, air gap ($l_g$) and stator inner diameter, the magnitude of the magnetic flux density in the air gap ($B_g$) can be determined. This flux density was used to calculate the phase back electromotive force ($E_{ph}$). The terminal phase voltage ($V∅$) was determined after calculating the stator wire impedance ($Z$) with a constant current of $3.63$ A. The study method was conducted by determining the design parameters, calculating the design variables, designing the generator dimensions using AutoCad and determining the magnetic flux density using FEMM simulation. The results show that the magnetic flux density in the air gap and the phase back emf $E_{ph}$ slightly decrease with increasing stator dimension because of increasing reluctance. However, the voltage drop is more dominant when the stator coil wire diameter is smaller. Thus, a larger diameter of the stator wire would allow terminal phase voltage ($V∅$) to become slightly larger. With a stator wire diameter of 1.29, 1.45 and 1.63 mm, the impedance values of the stator wire ($Z$) were 9.52746, 9.23581 and 9.06421 $Ω$ and the terminal phase voltages ($V∅$) were 220.73, 221.57 and 222.80 V, respectively. Increasing the power capacity ($S$) in the RFPMG design by increasing the diameter ($d$) of the stator wire will cause a significant increase in the percentage of the stator maximum current carrying capacity wire but the decrease in stator wire impedance is not significant. Thus, it will reduce the phase terminal voltage ($V∅$) from its nominal value.

Keywords: Permanent magnet generator, radial flux, flux density, voltage, power

© 2019 Penerbit UTM Press. All rights reserved
1.0 INTRODUCTION

There is significant potential in water energy due to extreme river water flow heads, which are commonly found in mountainous areas. These have been used to power hydropower (5–100 kW) and mini hydro (100 kW–1 MW) systems by utilizing generator technology and conventional turbines. The conventional generator has a high rotation speed ranging from 1500 to 3000 rpm. However, if implemented in a low head water catchment area, the turbine-generator spin may not produce the required voltage and nominal power.

Some research focusing on low head turbines has been completed. Erinoardi et al. [1] conducted an experiment to study a turbine screw coupled with a generator using two pairs of pulley reduction. The experiment used a water debit of 0.00068 m$^3$/s, with the generator spinning at a speed of 560 rpm and a turbine with a speed of 232 rpm producing a current of 33.1 mA with a voltage of 2.97 V. In the second pulley, the generator spun at 2457 rpm and the turbine with a speed of 946 rpm produced a current of 61.6 mA with a voltage of 4.5 V. Split reaction water turbines have potential applications for low micro hydro head installations. This turbine has mechanical and electrical efficiency in the range of 65–70% [2].

Compared to doubly-fed induction generators, Permanent Magnet sinkron generator (PMSG) has a higher efficiency and simpler structure because it has a permanent magnet instead of field winding in the rotor [3]. It is easier to change pole numbers in order to obtain the nominal rotational speed of the generator. One important aspect in the design of a permanent magnet generator is the flux density surrounding the stator coil [4]. The magnetic flux assembly of the stator coil ($B_0$) determines the output voltage and the power of the permanent magnet generator. The larger the magnetic flux density, the greater the output voltage and generator power [5]. Sharma et al. [6] argued that a permanent magnet generator has the ability to withstand the inrush current into the system when the system is connected to a synchronous input. In addition, permanent magnet synchronous generators also have advantages, such as no brush loss, no separate DC source for excitation, easy maintenance and the ability to protect themselves against overload and short-circuit [7]. Testing on a prototype of a three-phase axial double-sided permanent magnet generator can be done using 16 magnets on each rotor. Magnetostatic and magnetodynamic analyzes are performed with the finite element method using 250 W of power and a 5 mm air gap.

Conventional generators are operated using excitation systems, while for permanent magnet generators under load conditions, there is a decrease in magnetic flux (demagnetization) due to flux from the stator current generated by a fixed magnet [8]. However, in permanent magnet generators, there is no loss of brush power or power on the rotor. With a low air gap, the stator current becomes so small until the power loss on the stator can be neglected. This means that permanent magnet generators have high efficiency [9, 10]. In addition, the size and weight of the permanent magnet generator are smaller than the conventional generator because it does not require an excitation system [11].

Related to the study and development of a permanent magnet generator, Irasari [12] compared the characteristics of barium ferrite magnets (BaFe$_2$O$_4$) with neodymium iron boron (NdFeB). From their results, the flux of NdFeB was ten times larger than BaFe$_2$O$_4$. NdFeB also has the best price-to-power ratio compared to SmCo, ferrite and AlNiCo [13]. Herudin and Prasetyo [14] designed a permanent magnetic flux generator that produced ~7.91 V. At load conditions, the generator generated a voltage of 6.11 V with an efficiency of 32.84%. This performance needs to be reviewed for improvement. Ahmed and Ahmad [15] innovated the design using MATLAB Simulink to increase the efficiency of the axial permanent magnet generator that is applied to wind power plants. This method creates the characteristics of a permanent magnet generator in the construction process. Prasetijo and Waluyo [16] designed a ten poles single-phase axial permanent magnetic generator, type double-sided coreless stator, which resulted in a voltage of 87.25 V with a power of 322.84 VA. The output voltage of the generator is still lower than the nominal voltage of the electrical apparatus if it is implemented as a generator in a pico hydropower generating system.

This study will contribute to the process of designing a single-phase radial flux permanent magnet generator (RFPMG). The purpose of this study is to obtain the design of a single-phase RFPMG with a terminal voltage generator of 220 V, output power of 800 VA and a frequency of 50 Hz. The observed variables are the diameter of the stator winding wire, the voltage and output power of the generator. The analysis was performed using FEMM 4.2 to obtain the value of the magnetic flux density in the air gap.

Compared to findings from Herudin and Prasetyo [14] and Prasetyo and Waluyo [16], there are some developments that can be observed. The first study calculated the voltage drop on the stator winding to determine the value of the induction voltage (E) and the terminal voltage of the generator (V). Secondly, the resulting terminal voltage reached a nominal phase voltage of 220 V according to the nominal value of the low voltage network of PT.PLN. Thirdly, the magnetic flux density ($B_0$), magnetic flux ($\Phi$), electric motion ($E_{em}$), terminal phase voltage generator ($V_a$) and power ($P$) of three types of stator winding wire size were compared.

Figure 1 shows the rotor-stator of a RFPMG. An air gap is a distance between the magnet and the stator bore. The magnet is a flux generating magnet located on the rotor. Stator tooth is the stator part of the entanglement. There are six magnetic poles used to obtain a rotor speed of 1000 rpm at a frequency of 50 Hz. The yoke is the outer stator thickness.
2.0 METHODOLOGY

The stages and flow of the study activities are shown in Figure 2. It can be seen that the study is initiated by determining parameter values, calculating variable RFPMG dimensions, generator drawing construction in AutoCad and 2D finite element analysis in FEMM.

2.1 Radial Flux Permanent Magnet Generator Dimensions and Parameters

In the determination of the size of each part of the generator, the required input parameters are directly determined so that they can assist in the process of making the other parts of the generator. The following parameters influence the design of a permanent magnet synchronous generator of a single phase flux, as can be seen in Table 1.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Data</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frequency, f</td>
<td>50</td>
<td>Hz</td>
</tr>
<tr>
<td>Speed, n</td>
<td>1000</td>
<td>Rpm</td>
</tr>
<tr>
<td>Rotor Inner Diameter, Di</td>
<td>0.08</td>
<td>m</td>
</tr>
<tr>
<td>Magnet Thickness, tm</td>
<td>0.01</td>
<td>m</td>
</tr>
<tr>
<td>Air Gap, lg</td>
<td>0.003</td>
<td>m</td>
</tr>
<tr>
<td>Rotor Axial Length, L</td>
<td>0.08</td>
<td>m</td>
</tr>
<tr>
<td>Stator tooth Width, Wts</td>
<td>0.02</td>
<td>m</td>
</tr>
</tbody>
</table>

2.2 Designing Generator Design Variables

2.2.1 Rotor

The rotor of the RFPMG is a magnetic field generator because the permanent magnet is placed on the rotor part. Figure 3 shows the rotor dimensions of the RFPMG. The type of magnet used in this study is NdFeB (neodymium-iron-boron). The determination of variables for the rotor design includes:

- Number of Generator Poles (p)

There is a relationship between frequency and speed in determining the number of poles in the synchronous generator. The number of poles can be determined using equation (1).

$$f = \frac{np}{120}$$  \(1\)

where:
- \(f\) = frequency (Hz)
- \(n\) = rotational speed of the rotor (rpm)
- \(p\) = number of magnetic poles
B. Rotor and Stator Pole Ranges
The rotor pole range \( \tau \) is the actual magnet span, while the stator pole range \( \tau_s \) is the circumferential length of the magnetic pole can and be calculated using equations (2) and (3) below:

\[
\tau_p = \frac{n \times D_{si}}{D_{ri}} \quad (2)
\]
\[
\tau_r = \tau_m = \tau_p \times 0.75 \quad (3)
\]

C. Distance Between Magnets \( \tau_r \)
Determining the distance between magnets can refer to equation (4) by using previously known variables:

\[
\tau_f = \tau_p - \tau_r \quad (4)
\]

D. Permeance Coefficient \( P_c \)
The following equations are used to determine the value of the Pc:

\[
P_c = \frac{t_m}{L_{cB}} \quad (5)
\]
\[
C_p = \frac{A_m}{A_g} = \frac{2a_m}{1 + a_m} \quad (6)
\]
\[
a_m = \frac{t_m}{t_p} \quad (7)
\]

where:
- \( t_m \) = magnet thickness (m)
- \( C_B \) = factor of flux concentration
- \( A_m \) = magnitude of the area facing the stator
- \( A_g \) = constant area of air gap

E. Effective Length and Area of Rotor Pole
Equations (8) and (9) are used to calculate the effective core length value \( L_i \) and the area of the rotor pole \( A_{pr} \):

\[
L_i = L_iK_{stack} \quad (8)
\]
\[
A_{pr} = \tau_rL_i \quad (9)
\]

F. Outer Diameter of Rotor
Equation (10) can be used to determine the outside diameter of the rotor:

\[
D_{ro} = 2 \times t_m + D_{ri} \quad (10)
\]

2.2.2 Stator
The stator itself is part of a generator that is usually static. Figure 4 shows the stator variables and its dimensions. The determination of variable stator design includes:

A. Inner Diameter Stator
The inner diameter of the stator is determined by adding the air gap width to the outer diameter of the rotor, as displayed in equation (11):

\[
D_{si} = 2 \times t_g + D_{ro} \quad (11)
\]

![Figure 4 Stator GSMPF specification](image)

B. Number of Slots
The number of slots on the stator can be calculated using equation (12):

\[
S_s = p.q.m \quad (12)
\]

The number of slots in one phase \( S_i \) and the number of slots that can be magnetized by a single pole \( S_k \) can be determined using equations (13) and (14):

\[
S_f = \frac{S_i}{m} \quad (13)
\]
\[
S_k = \frac{S_i}{k} \quad (14)
\]

C. Inner Slot Width \( b_{si} \)
Based on Figure 3, \( b_{si} \) is the radial length of the inner slot area. Therefore, the value of \( b_{si} \) can be determined using equation (15):

\[
b_{si} = \left( \frac{\pi D_{si} + 2\Delta t + 2h_d}{S_s} \right) - W_{ts} \quad (15)
\]

D. Area of Stator Slot
Before determining the area of the stator slot, it is important to determine the type of wire used in this study because it will affect the value of the conductor diameter (equations (16)–(19)):

\[
A_{ss} = \frac{(A_mN_s)}{P_F} \quad (16)
\]
\[
A_w = \frac{h}{f} \quad (17)
\]
\[
d_w = \sqrt{\frac{(4A_w)}{\pi}} \quad (18)
\]
\[
J = \frac{\Delta_{max}}{A_w} \quad (19)
\]

E. Width of Outside of Stator Slot \( b_{s2} \)
After \( b_{si} \) is obtained, it can determine the value of \( b_{s2} \), which is the radial length of the outer slot area (equation (20)):

\[
b_{s2} = \sqrt{\frac{4A_{ss} \tan \frac{\pi}{S_s} + b_{si}}{2}} \quad (20)
\]
F. Stator Slot Height
After the above equation is known, it can then determine the height of the stator slot by using equation [21]:

\[ h_s = \frac{2A_{ba}}{b_{s1} + b_{s2}} \]  

(21)

G. Middle Value of Radial Length of Stator Slot (Wss)
Wss is the value that will be used to calculate the value of \( k_c \) in the determination of the value \( B_p \). The value of \( W_{ss} \) itself is calculated using equation (22) as follows:

\[ W_{ss} = \frac{b_{s1} + b_{s2}}{2} \]  

(22)

H. Long Range of Stator Slot Area
The range for the length of the stator slot area \( (\tau_s) \) is the sum of the length \( b_{s1} \) and length \( W_{ss} \) (equation (23)):

\[ \tau_s = b_{s1} + W_{ss} \]  

(23)

I. Value of Flux Density (Bg) in Generator
The flux density value \( (B_g) \) can be determined after the leakage value \( (k_{ml}) \) and the Carter coefficient \( (k_c) \), which are calculated as follows:

a. Determining Leakage Value \( (k_{ml}) \)
The value of \( k_{ml} \) be calculated using equation (24):

\[ k_{ml} = 1 + \frac{4t_m}{\rho_{st} \cdot a_m \cdot t_p} \ln \left[ 1 + \frac{\rho_{st}}{((1 - \sigma_m) t_p)} \right] \]  

(24)

b. Carter Coefficient \( (k_c) \)
In the determination of the value of \( k_c \), \( l_g \) is an unknown parameter. The value of \( l_g \) is the effective air gap length, which can be calculated using equations (25) and (26):

\[ l_g = l_g + \frac{l_m}{\mu_0} \]  

(25)

\[ k_c = \left[ 1 - \frac{W_{ss}}{\tau_s} + \frac{4l_g'}{\rho_{st}} \ln \left( 1 + \frac{W_{ss} \cdot \pi}{4l_g'} \right) \right] - 1 \]  

(26)

c. Value of \( B_g \)
The magnetic flux density, \( B_g \) can be calculated using equation (27):

\[ B_g = \frac{(c_0)}{\left(1 + \frac{\mu_0 \cdot k_c \cdot k_{ml}}{\gamma_c} \right)} B_r \]  

(27)

J. Distribution Factor
The value of the distribution factor can be calculated using equations (28)–(30):

\[ \beta = \frac{180}{S_s \cdot m} \]  

(28)

\[ c = \frac{S_s}{p \cdot m} \]  

(29)

\[ k_d = \frac{\sin (c \cdot B/2)}{c \cdot (\sin B/2)} \]  

(30)

K. Magnetic Flux Value
Equation (31) can be used to determine the magnetic flux value:

\[ \Phi = B_g A_{pr} \]  

(31)

where \( A_{pr} \) is the magnetic surface area.

L. Width of Yoke Stator (Ys) and Stator Outside Diameter (Dso)
The yoke stator is a buffer of stator construction or is often called the stator frame. The stator yoke can be calculated using equations (32) and (33):

\[ Y_s = \frac{a}{2 \cdot c \cdot r_t} \]  

(32)

\[ D_{so} = D_{si} + 2(h_s + h_{as} + h_w + Y_s) \]  

(33)

2.3 Determination of Electricity Variables of Generator Output
The determination of electricity variables of generator output includes:

A. Phase Back Emf (Eph) Generator Value
The value of Eph is represented during open-circuit conditions. Equation (34) can be used to calculate Eph:

\[ E_{ph} = 4.44 \times \pi \times N_s \times k_w \times S_f \times \Phi \]  

(34)

B. Phase Current (Iph) and Phase Resistance (Rph)
The Iph and Rph values are used to determine the output voltage of the generator. Equations (35) and (36) can be used to calculate Iph and Rph:

\[ I_{ph} = A_{w} J \]  

(35)

\[ R_{ph} = \frac{\rho_{w} x n_s x l_p x S_f}{\sqrt{m}} \]  

(36)

C. Reactance and Impedance Value Generator
The reactance value in the generator can be calculated using equation (37). Once the resistance and reactance values are obtained, the value of the generator impedance can be computed using equation (38):

\[ X_L = 4. m \cdot \mu_0 \cdot f \left( \frac{S_s \cdot k_{ml}^2}{\pi p P} \right) \]  

(37)

\[ Z_{ph} = Z_{ph} = \sqrt{R_{ph}^2 + X_L^2} \]  

(38)
D. Phase Voltage Output Value
The output voltage value can be computed using the following formula:

\[ V_o = E_{ph} - I_{ph}R_{ph} \]  \hspace{1cm} (39)

E. Output Power Generator
The output power refers to the apparent power that is generated by the multiplication of voltage and electric current. Equation (40) is used to determine the apparent power:

\[ S = V \times I \]  \hspace{1cm} (40)

3.0 RESULTS OF SIMULATION AND DISCUSSION
In this study, there are several developments compared to Herudin [13] and Prasetyo [15]. The first study was to calculate the voltage drop on the stator winding so that it can determine the value of the phase back emf \( E_{ph} \) and the terminal phase voltage of the generator \( V_o \). Second, the resulting terminal voltage reached a nominal phase voltage of 220 V according to the nominal value of the low voltage network of PT. PLN. Third, the values of magnetic flux density \( B_g \), magnetic flux \( \phi \), phase back emf \( E_{ph} \), terminal voltage generator \( V_o \) and power \( S \) for three types of stator winding wire size were calculated and compared.

The generator design uses three wire sizes by referring to the American Wire Gauge (AWG), namely, AWG 14, AWG 15 and AWG 16, which were equivalent to wire diameters of 1.63, 1.45 and 1.29 mm, respectively, as stator windings. By increasing the size of the wire in the stator winding, the generator power output capacity was greater due to the increased in the current capacity that can be passed through the stator coil as an armature coil by producing the back emf on the generator. This affected the stator dimension. The type of wire conductor did not affect the size of the rotor dimension but affected the stator dimension of the generator. Table 2 shows the dimensions of a permanent magnetic flux generator using the three wires as a stator coil. These dimensions were derived from the calculations using the equations in the sub methodology.

From Table 2, it can be seen that an increment in the power capacity \( S \) of the generator resulted by increasing the diameter of the stator coil wire had an impact on the several stator dimensions, i.e., the outer diameter of the stator \( D_{so} \), the height of the stator teeth \( h_s \) and the length of the outer stator slot \( b_{s2} \).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Dimension (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>AWG 14</td>
</tr>
<tr>
<td>D</td>
<td>0.02</td>
</tr>
<tr>
<td>Dr</td>
<td>0.08</td>
</tr>
<tr>
<td>Dho</td>
<td>0.1</td>
</tr>
<tr>
<td>fp</td>
<td>0.04187</td>
</tr>
<tr>
<td>fr</td>
<td>0.0314</td>
</tr>
<tr>
<td>Tm</td>
<td>0.01</td>
</tr>
<tr>
<td>Lg</td>
<td>0.003</td>
</tr>
<tr>
<td>L</td>
<td>0.08</td>
</tr>
<tr>
<td>Li</td>
<td>0.072</td>
</tr>
<tr>
<td>Dsi</td>
<td>0.106</td>
</tr>
<tr>
<td>Dso</td>
<td>0.16706</td>
</tr>
<tr>
<td>Wfs</td>
<td>0.02</td>
</tr>
<tr>
<td>hs</td>
<td>0.02239</td>
</tr>
<tr>
<td>rs</td>
<td>0.05861</td>
</tr>
<tr>
<td>b1s</td>
<td>0.03861</td>
</tr>
<tr>
<td>b2s</td>
<td>0.06447</td>
</tr>
<tr>
<td>hso, hw</td>
<td>0.001</td>
</tr>
<tr>
<td>y</td>
<td>0.00514</td>
</tr>
</tbody>
</table>

With fixed magnetic flux \( \phi \) and back emf \( E_{ph} \), an increment in the power capacity of the RFPMG is to increase the outer diameter of the stator \( D_{so} \).

Figure 5 shows a description of the design dimension of the permanent magnetic flux generator from Table 2. The inner part is the rotor dimension while the outer part is the stator dimension. The permanent magnet acts as a magnetic flux generator that lies in the rotor portion instead of the field coil. Between the stator teeth and permanent magnet is an air gap \( l_g \).
3.1 Finite Element Simulation and Analysis

This simulation and analysis were achieved by using FEMM software to determine the magnetic flux ($B_g$) density of the air gap. The design dimension of the RFPMG was used as a simulation base with the following steps.

A. Design in FEMM Software

To obtain the magnetic flux ($B_g$) density in the air gap, the generator design was illustrated in the FEMM software by labeling the material of each component of the generator. The selected materials can be seen in Table 3.

<table>
<thead>
<tr>
<th>Generator Components</th>
<th>Materials</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rotor Shaft</td>
<td>Mild Steel</td>
</tr>
<tr>
<td>Rotor</td>
<td>Aluminum 1100</td>
</tr>
<tr>
<td>Permanent Magnet</td>
<td>NdFeB 32 MgOe</td>
</tr>
<tr>
<td>Stator</td>
<td>M-19 Steel</td>
</tr>
</tbody>
</table>

Aluminum was chosen because it has a very strong mechanical alloy that can reduce thermal conductivity and its resistance to corrosion. Silicon steel has a steel content that can reduce eddy current and reduce hysteresis core lamination.

B. Meshing Design on FEMM Software

The next stage was the prototype meshing using FEMM software. Meshing is a tool to define the boundaries of the materials defined in the design. The material boundary of each component was limited using yellow webs (mesh). The image meshing design is displayed in Figure 6.

C. Simulation of Magnetic Flux in Air Gap

The simulations were performed on three generator designs: each using AWG 14, AWG 15 and AWG 16 wires of 160 loops per slot to keep the back emf ($E_{ph}$) relatively fixed.

Figure 7 shows the simulation results of the design of the RFPMG. The color contour shows the magnitude of the magnetic flux density by the order of magnetic flux density levels from small to large: blue, green, yellow, orange and purple. The lowest flux is in the air (blue) while the highest is in the yoke stator (purple) because the yoke stator is made of silicon steel that has higher permeability. Magnetic permeability is the ability of a material to pass a magnetic force line based on equation (41).

$$\mu = \mu_0 \mu_r$$

where:
- $\mu$ = permeability
- $\mu_0$ = permeability vacuum, $3.14 \times 10^{-7}$ Wb/A.m
- $\mu_r$ = relative permeability of materials

The relative permeability of silicon steel has a value of ~1500 times that of air. Thus, it can be used to explain the magnetic flux density of the yoke, which was larger than the flux density in the air gap region.
The stator teeth exhibit an orange color, showing that the level of the magnetic flux density was lower than the yoke. This was due to the back emf on the stator coil induced flux in the direction against the flux of the permanent magnet.

 Flux in the air gap between the magnetic pole and the stator pole (stator teeth) was required for the calculation of the back emf \( (E_{ph}) \) on the stator coil. To find the flux, five test points along the air gap under the stator pole were taken. Figure 8 shows the test point for finding the magnetic flux density \( (B_g) \).

 Figure 8 also shows that the flux density in the stator teeth (stator coil location) is smaller than the density of the yoke flux. This is because the induced voltage produces the opposite flux from the direction of permanent magnetic flux, as shown in equation (42):

\[
e = -\frac{d\phi}{dt}
\]  

 D. Simulation of Single-Phase RFPMG Design with AWG Wire 14

 Using the above steps, the magnetic flux density \( (B_g) \) in the single-phase RFPMG design air gap with the stator coil using the AWG 14 wire was determined. The results are shown in Figure 9 with test points 1 to 5 being the points on the air gap (can refer to Figure 8 from left to right).

 The value of the coordinates of the test point used and the resulting flux density value can be seen in Table 4. The \( B_g \) value at five test points located under the stator pole (stator teeth) has a value between 0.5 and 0.6 T.

<table>
<thead>
<tr>
<th>Test point</th>
<th>Nilai ( B_g ) (T)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.529047</td>
</tr>
<tr>
<td>2</td>
<td>0.527197</td>
</tr>
<tr>
<td>3</td>
<td>0.523745</td>
</tr>
<tr>
<td>4</td>
<td>0.527854</td>
</tr>
<tr>
<td>5</td>
<td>0.530051</td>
</tr>
</tbody>
</table>

The \( B_g \) value is determined from the average \( B_g \) value in the five test points of 0.52958 T.

 Figure 10 shows the waveform of the air gap flux density distribution from one side middle magnet pole adjacent to the other side (pole-pitch) that show a \( \frac{1}{2} \) period waveform.

Figure 7 Simulation of magnetic flux density generator design

Figure 8 Simulation of magnetic flux density with five test points in the air gap

Figure 9 Graph of GSMPFR testing with AWG 14

Figure 10 Waveform of air gap flux density distribution

Table 4 Air gap test point with AWG 14
3.2 RFP MG Output Variable Calculation

The RFP MG output variables include phase back emf ($E_{ph}$), phase current ($I_{ph}$), phase voltage ($V_\phi$) and output power ($S$). The calculation of RFP MG output variables is achieved with the following steps.

A. Determining Phase Back Emf ($E_{ph}$)

The predetermined $B_g$ value through the simulation was used to calculate the $\Phi$ flux and phase back emf ($E_{ph}$) using equation (34).

$$\Phi = B_g \cdot A_{pr} = 0.52918 \times 0.00226 = 0.001196 \text{ Wb}$$

$$E_{ph} = 4.44 \times 50 \times 160 \times 1 \times 6 \times 0.001196 = 254.89 \text{ V}$$

Figure 11 shows the induced voltage (back-emf) as a sinusoidal waveform.

![Back-Emf waveform](image)

B. Determining $I_{ph}$ and $R_{ph}$ Generator

The phase current value ($I_{ph}$) was used to find the maximum current value generated from the conducting wire using equation (35).

$$I_{ph} = A_w \cdot J = 2.08567 \times 10^{-6} \times 2828831.93454 = 5.9 \text{ A}$$

where $A_w$ is the wire cross-sectional area of AWG 14 in units of m$^2$ (wire diameter AWG 14 = 1.29 mm) and J is the current density of AWG 14 in units of A/m$^2$.

Since in this study, the generator output was limited to a 220 V output voltage and 800 VA output power, the current used to achieve the generator output value can be calculated by the equation below:

$$I_{ph} = \frac{S}{V} = \frac{800}{220} = 3.63 \text{ A}$$

$$\%I_{max} = \frac{3.63}{5.9} = 61.52542 \%$$

The desired value of per phase current was equal to 3.63 A or 61.52542% from the maximum current value of the AWG 14 wire. The per phase resistance ($R_{ph}$) was used to find the impedance value of the generator output using equation (36).

$$R_{ph} = \frac{\rho_w \times N_s \times L_s \times S_s}{A_w \times m}$$

where $\rho_w$ is density type of mass (Q.m), $N_s$ is the number of turns, $L_s$ is the length of one winding (m), $S_s$ is the number of stator slots and $m$ is the number of phases. The value of the stator coil resistance is:

$$R_{ph} = \frac{1.72E-08 \times 166 \times (2 \times (0.02 + 0.072)) \times 6}{2.08567E-08} = 1.51134 \text{ Ohm}$$

C. Determining Reactance Value and Impedance Generator

Before determining the output impedance value of the generator, the value of reactance ($X_L$) was calculated using equation (37).

$$X_L = 4.4 \times m \times \mu_0 \cdot f \times \left( \frac{(N_w \times A_w)^2}{p \times p} \right) \times \frac{S_w \times L_s}{K_s \times L_g}$$

where $m$ is the number of phases, $K_w$ is the winding factor, which is the ratio between the coil dimension and the stator slot dimension, $p$ is the number of pairs of stator curves, $S_w$ is the slot per pole, $L$ is the effective length of the rotor, $K_s$ is Carter's coefficient, i.e., the number of slots per phase with air gap width and $L_g$ is the air gap width. Thus, the value of the stator coil reactance can be computed by the following equation:

$$X_L = 4 \times 1 \times 4 \times 3.14 \times 10^{-7} \times 50 \left( \frac{160 \times 1}{3.14} \right) \times \frac{1 \times 0.072}{1.91056 \times 0.003} = 8.9373 \text{ } \Omega$$

By knowing the value of resistance and stator coil reactance, the output impedance of the generator was calculated using equation (38).

$$Z_{ph} = \sqrt{R_{ph}^2 + X_L^2} = \sqrt{1.51134^2 + 8.93732^2} = 9.06421 \text{ } \Omega$$

D. Determining the Output Phase Voltage

After obtaining the value of the back emf ($E_{ph}$), the phase current ($I_{ph}$), the phase impedance ($Z_{ph}$) and the value of the output terminal phase voltage generator ($V_\phi$) can be calculated by subtracting the back emf value by the voltage drop on the stator coil using equation (39).

$$V_\phi = E_{ph} - I_{ph} \cdot Z_{ph} = 255.74 - (3.63 \times 9.06421) = 222.8 \text{ V}$$

E. Determining Generator Output Power

The final step was to determine the output power of the generator by multiplying the output voltage of the generator with the phase current obtained. Below is the calculation to find the output power generator with equation (40).

$$S = V \times I = 222.8 \text{ V} \times 3.63 = 808.8 \text{ V}$$
By performing the same calculation procedure for stator wind types AWG 15 and AWG 16, the comparison of variable values was made and summarized, as shown in Table 5.

From Table 5, it is known that the magnetic flux ($B_g$) tends to slightly decrease sequentially from the use of the AWG 16 ($d = 1.29$ mm), AWG 15 ($d = 1.45$ mm) and AWG 14 ($d = 1.63$ mm) wires. The larger the diameter of the wire in the stator coil with the same rotor and magnetic dimensions, the smaller the flux density and the magnetic flux. By referring to Figure 5 on the design parameters and Table 2, the larger the diameter of the wire on the stator coil, the larger the stator height ($h_s$). As the height of the stator teeth ($h_s$) increases, the length of the outer stator slot ($b_{22}$) also increases in size. By increasing the size of $b_{22}$ with reference to equation (22), the size of the middle length of the radial slot stator ($W_s$) also increases. Based on equation (26), the coefficient of the charter ($K_C$) increases if the $W_s$ value increases. The relationship between these variables can be explained clearly using equation (27):

$$B_g = \frac{(C_0)}{(1 + \frac{\mu_s}{\mu_A} C_p)} B_r$$

From equation (27), the other parameters were fixed. The concentration factor ($C_0$) of equation (6) was determined by the surface area of the magnet facing the stator ($A_{m}$) and the air gap width constant ($A_g$). In the design of the magnetic dimension and air gap, the values of $A_{m}$ and $A_g$ remained so that the value of $C_0$ also remained. The $\mu$ parameter is the relative permeability of a NdFeB N32 magnet (1.1). The $kml$ parameter is a magnetic flux leakage variable based on equation (24), whereby its value was influenced by the rotor and magnetic dimensions. Because the dimensions of the rotor and magnet were fixed, then the $kml$ value was also fixed. From equation (5), the value of the $P_c$ (permeance coefficient constant) was influenced by the magnetic thickness ($t_m$) and air gap width ($l_g$), whereas both were fixed so that the $P_c$ value was also fixed. The parameter $B_r$ was the magnetic flux density of the NdFeB N32 magnet. The $B_r$ value is 1.

Another explanation can be reached from the concept of reluctance. The longer the material, the greater the reluctance, as shown below:

$$R = \frac{L}{\mu A}$$

where:

$R = \text{reluctance}$

$\mu = \text{permeability}$

$A = \text{cross-sectional area}$

The greater the stator outside diameter ($D_{so}$), the greater the reluctance increase that causes the magnetic flux decrease.

<table>
<thead>
<tr>
<th>Table 5 Comparison of generator parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Parameter</strong></td>
</tr>
<tr>
<td>---------------</td>
</tr>
<tr>
<td></td>
</tr>
<tr>
<td>$B_g$</td>
</tr>
<tr>
<td>$\phi$</td>
</tr>
<tr>
<td>$E_{ph}$</td>
</tr>
<tr>
<td>$Z$</td>
</tr>
<tr>
<td>$I$</td>
</tr>
<tr>
<td>$V_\phi$</td>
</tr>
<tr>
<td>$S$</td>
</tr>
<tr>
<td>$V_{drop}$</td>
</tr>
<tr>
<td><strong>Maximum current</strong></td>
</tr>
</tbody>
</table>

From Table 5, it is also known that when the dimensions of the coil wire increased, the back emf ($E_{ph}$) on the stator coil also decreased, but the generator terminal voltage was increased. In accordance with equation (39), the smaller the diameter of the stator coil wires, the greater the stator coil impedance. This caused the voltage drops across the stator coil to be greater, so that the terminal voltage becomes smaller. Thus, the decrease in back emf ($E_{ph}$) of the stator coil was smaller than the drop in voltage ($\Delta V$) on the stator coil. The larger the diameter of the stator coil wire, the larger the terminal voltage ($V_{\phi}$).

By referring to Table 5 and the discussion above, the relation of the stator wire diameter ($d$), the stator wire impedance ($Z$), the maximum current carrying capacity ($I$) and the voltage drop on the AWG wires 16, 15 and 14 can be determined, as shown in Table 6.

Table 6 shows that the increase in wire diameter from AWG 16 to 15 ($1.29$ to $1.45$ mm) and from AWG 15 to 14 ($1.45$ to $1.63$ mm) will cause changes, namely, an increase in the maximum current carrying capacity, a decrease in wire impedance and an increase in maximum voltage drop. The percentage changes can be seen in Table 7.

From Table 6, it is known that increasing the diameter ($d$) of the stator wire will increase the maximum carrying capacity ($I$), thereby increasing the RFPMG power capacity ($S$).
Based on Table 7, increasing the power capacity (S) in the RFPFG design by increasing the diameter (d) of the stator wire with a constant value in the phase back emf (Eph) variable, the dimensions of the rotor, permanent magnet, air gap (l0) and inner diameter stator must be paid attention to the voltage drop (ΔV) of the stator wire to obtain the nominal value of the phase terminal voltage.

Increasing the diameter of the stator wire will cause a significant increase in the percentage of the stator maximum current carrying capacity wire but the decrease in stator wire impedance is not significant. For the examples of Tables 6 and 7, an increase in the stator wire diameter from AWG 16 (d = 1.29 mm) to AWG 15 (d = 1.45 mm) increases the maximum current carrying capacity of 27.03%, but the impedance reduction is only 3.06%. This will cause an increase in voltage drop (ΔV) of 23.14%, so that it will reduce the phase terminal voltage (Vt) from its nominal value.

### 4.0 CONCLUSION

In design of single-phase radial flux permanent magnet generator, the wire dimensions of the stator coil affected the dimensions of the stator's outer diameter (Ds), the height of the stator gear (hs), the length of the outer stator slot (D2s) and the yoke width of the stator (Ys). The increment in the dimension of the outer diameter of the stator (Ds) due to the larger diameter of the stator coil wire by constant values of the dimensions of the rotor, permanent magnet, air gap (l0), stator height (hs) and stator diameter (Ds), causing magnetic flux density (Bs) and the magnetic flux (ψ) in the air gap tends to decrease the value, so that value of the back emf (Eph) decreased too. However, as the diameter of the stator coil wire decreased, value of drop voltage (ΔV) became significant, so terminal voltage (VT) increased with the larger diameter of the stator coil wire. From the result of simulation and discussions proved that the stator wire with diameters of 1.29 mm (AWG 16), 1.45 mm (AWG 15) and 1.63 mm (AWG 14) had air gap fluxes (Bs) of 0.52995, 0.52961 and 0.52958 T that produced terminal voltages of 220.73, 221.57 and 222.80 V, respectively. Another result, increasing the power capacity (S) in the RFPFG design by increasing the diameter (d) of the stator wire will cause a significant increase in the percentage of the stator maximum current carrying capacity wire but the decrease in stator wire impedance is not significant. So that it will reduce the phase terminal voltage (Vt) from its nominal value.

### References


### Table 6 Comparison derivative variables of AWG 16, 15 and 14

<table>
<thead>
<tr>
<th>Diameter (mm)</th>
<th>AWG 16</th>
<th>AWG 15</th>
<th>AWG 14</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.29</td>
<td>1.45</td>
<td>1.63</td>
<td></td>
</tr>
</tbody>
</table>

### Table 7 Percentage changes in parameters

<table>
<thead>
<tr>
<th>Increase in diameter (%)</th>
<th>AWG 16 to 15</th>
<th>AWG 15 to 14</th>
</tr>
</thead>
<tbody>
<tr>
<td>12.40</td>
<td>12.41</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Increase in maximum current (%)</th>
<th>AWG 16 to 15</th>
<th>AWG 15 to 14</th>
</tr>
</thead>
<tbody>
<tr>
<td>27.03</td>
<td>25.53</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Decrease in impedance (%)</th>
<th>AWG 16 to 15</th>
<th>AWG 15 to 14</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.06</td>
<td>1.86</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Increase in voltage drop (%)</th>
<th>AWG 16 to 15</th>
<th>AWG 15 to 14</th>
</tr>
</thead>
<tbody>
<tr>
<td>23.14</td>
<td>23.20</td>
<td></td>
</tr>
</tbody>
</table>


